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resources

Visit the companion website at resources.corwin.com/mathlessonplanning/6-8 for downloadable resources.